

Package ‘MultiATSM’

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Type Package

Title Multicountry Term Structure of Interest Rates Models

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Description Estimation routines for several classes of affine term structure of interest rates models. All the models are based on the single-country unspanned macroeconomic risk framework from Joslin, Priebsch, and Singleton (2014) <[doi:10.1111/jofi.12131](https://doi.org/10.1111/jofi.12131)>. Multicountry extensions such as the ones of Jotikasthira, Le, and Lundblad (2015) <[doi:10.1016/j.jfineco.2014.09.004](https://doi.org/10.1016/j.jfineco.2014.09.004)>, Candelon and Moura (2021) <<http://hdl.handle.net/2078.1/249985>>, and Candelon and Moura (2023) <[doi:10.1016/j.econmod.2023.106453](https://doi.org/10.1016/j.econmod.2023.106453)> are also available.

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RoxygenNote 7.1.1

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Bias_Correc_VAR

*Estimate an unbiased VAR(1) using stochastic approximation (Bauer, Rudebusch and Wu, 2012)***Description**

Estimate an unbiased VAR(1) using stochastic approximation (Bauer, Rudebusch and Wu, 2012)

Usage

```
Bias_Correc_VAR(
  ModelType,
  BRWinputs,
  RiskFactors,
  N,
  Economies,
  FactorLabels,
  GVARinputs = NULL,
  JLLinputs = NULL,
  ev_restr = 1,
  nargout = 4
)
```

Arguments

ModelType	string-vector containing the label of the model to be estimated
BRWinputs	List containing the following necessary inputs for the estimation of the BRW model: <ol style="list-style-type: none"> 1. flag_mean: flag whether mean- (TRUE) or median- (FALSE) unbiased estimation is desired. Default is set to TRUE; 2. gamma: adjustment parameter. Value parameters should vary between 0 and 1. Default is set to 0.5; 3. N_iter: number of iterations used in the stochastic approximation algorithm after burn-in. Default is set to 5,000; 4. N_burn: number of burn-in iterations used in the stochastic approximation algorithm. Default is set to 0.15*N_iter; 5. B: number of bootstrap samples per iteration to calculate noisy measure of mean/median of the OLS estimator. Default is set to 50; 6. check: flag whether the user wishes to perform the closeness check. Default is set to TRUE; 7. B_check: number of bootstrap samples used in the closeness check. Default is set to 100,000.
RiskFactors	time series of the risk factors (T x F)
N	number of country-specific spanned factors (scalar)
Economies	string-vector containing the names of the economies which are part of the economic system
FactorLabels	string-list based which contains the labels of all variables present in the model
GVARinputs	inputs used in the estimation of the GVAR-based models (see "GVAR" function). Default is set to NULL
JLLinputs	inputs used in the estimation of the JLL-based models (see "JLL" function). Default is set to NULL
ev_restr	largest eigenvalue restriction under the P-measure. Default is set to 1
nargout	number of elements present in the list of outputs. Default is set to 4

Value

Bias-corrected VAR parameters based on the framework of Bauer, Rudebusch and Wu (2012). The list contains:

1. Phi_tilde estimated coefficient matrix (F x F);
2. mu_tilde: estimated intercept (F x 1);
3. V_tilde: estimated variance-covariance matrix (F x F);
4. dist: root mean square distance (scalar);
5. Phi_sample: sample estimated variance-covariance matrix used in the checks (F x F x B_check)
- this output is reported if nargout is set to 5.

References

Bauer, Rudebusch and, Wu (2012). "Correcting Estimation Bias in Dynamic Term Structure Models"

This function is based on the "est_unb_var" Matlab function available at Cynthia Wu's website (<https://sites.google.com/view/jingcynthiawu/>).

Examples

```

data(CM_Factors)
Factors <- t(RiskFactors[1:7,])

BRWinputs <- list()
BRWinputs$flag_mean <- TRUE
BRWinputs$gamma <- 0.4
BRWinputs$N_iter <- 1000
BRWinputs$N_burn <- 100
BRWinputs$B <- 10
BRWinputs$check <- 1
BRWinputs$B_check <- 5000

Economies <- "China"
N <- 3
ModelType <- "JPS"
FactorLabels <- NULL

BRWpara <- Bias_Correc_VAR(ModelType, BRWinputs, Factors, N, Economies, FactorLabels)

```

Bootstrap	<i>Generates the bootstrap-related outputs</i>
-----------	--

Description

Generates the bootstrap-related outputs

Usage

```
Bootstrap(
    ModelType,
    ModelParaPE,
    NumOutPE,
    mat,
    Economies,
    InputsForOutputs,
    FactorLabels,
    DataFrequency,
    vararginPE,
    JLLinputs = NULL,
    GVARinputs = NULL,
    BRWinputs = NULL
)
```

Arguments

ModelType	string-vector containing the label of the model to be estimated
ModelParaPE	point estimate from the model parameters (see the outputs of the "Optimization" function)
NumOutPE	point estimate from the numerical outputs (see the outputs of the "NumOutputs" function)
mat	vector of maturities (in years) used in the estimation
Economies	string-vector containing the names of the economies which are part of the economic system
InputsForOutputs	list containing the desired inputs for the construction of IRFs, GIRFs, FEVDs, and GFEVDs.
FactorLabels	string-list based which contains the labels of all the variables present in the model
DataFrequency	character-based vector: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually"
vararginPE	list containg starting values and constraints (see arguments of the "Optimization" function)
JLLinputs	list of necessary inputs for the estimation of JLL-based models (see "JLL" function)

GVARinputs	list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function)
BRWinputs	list of necessary inputs for performing the bias-corrected estimation (see "Bias_Correc_VAR" function)

Value

list containing the following elements:

- list of model parameters for one each one the draws;
- list of numerical outputs (IRFs, GIRFs, FEVDs, GFEVDs) for each one of the draws;
- Confidence bands for the chosen level of significance.

References

This function is a modified and extended version of the "VARirbound" function from "A toolbox for VAR analysis" by Ambrogio Cesa-Bianchi (<https://github.com/ambropo/VAR-Toolbox>)

Examples

```
# See examples in the vignette file of this package (Section 4).
```

BR_jps_out

Replications of the JPS (2014) outputs by Bauer and Rudebusch (2017)

Description

Unspanned macro risk model outputs by Bauer and Rudebusch (2017)

Usage

```
data("BR_jps_gro_R3")
```

Format

Unspanned macro risk model outputs by Bauer and Rudebusch (2017)

est.llk summary list of log-likelihood estimations

M.o time series of unspanned factors

pars additional summary list of log-likelihood estimations

W Weight matrix that results from principal components analysis

Y time series of bond yields

N total number of risk factor of the model (spanned and unspanned)

R total number of spanned factor of the model

References

Bauer, M. and Rudebusch, G. "Resolving the Spanning Puzzle in Macro-Finance Term Structure Models"

DatabasePrep

Prepare the GVARFactors database

Description

Prepare the GVARFactors database

Usage

```
DatabasePrep(
  t_First,
  t_Last,
  Economies,
  N,
  FactorLabels,
  ModelType,
  Wgvar = NULL,
  DataPathMacro = NULL,
  DataPathYields = NULL
)
```

Arguments

t_First	sample starting date (yyyy-mm-dd)
t_Last	sample last date (yyyy-mm-dd)
Economies	string-vector containing the names of the economies which are part of the economic system
N	number of country-specific spanned factor (scalar)
FactorLabels	list containing the factor labels
ModelType	string-vector containing the label of the model to be estimated
Wgvar	GVAR transition matrix (CxC), if GVAR type model is chosen; default is set to NULL.
DataPathMacro	path of the Excel file containing the macroeconomic data (if any). The default is linked to the Excel file available in the package.
DataPathYields	path of the Excel file containing the yields data (if any). The default is linked to the Excel file available in the package.

Value

List of the risk factor set used in the estimation of the GVAR model

List containing the risk factor set used in the estimation of the GVAR-based models

Examples

```
DomVar <- c("Eco_Act", "Inflation")
GlobalVar <- c("GBC", "CPI_OECD")
t0 <- "2006-09-01"
tF <- "2019-01-01"
Economies <- c("China", "Brazil", "Mexico", "Uruguay", "Russia")
N <- 3
ModelType <- "JPS jointQ"
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)

GVARFactors <- DatabasePrep(t0, tF, Economies, N, FactorLabels, ModelType)
```

DataForEstimation	<i>Retrieve data from Excel and build the database used in the model estimation</i>
-------------------	---

Description

Retrieve data from Excel and build the database used in the model estimation

Usage

```
DataForEstimation(
  t0,
  tF,
  Economies,
  N,
  FactorLabels,
  ModelType,
  DataFrequency,
  W_type = NULL,
  t_First_Wgvar = NULL,
  t_Last_Wgvar = NULL,
  DataPathMacro = NULL,
  DataPathYields = NULL,
  DataPathTrade = NULL
)
```

Arguments

t0	Sample starting date (yyyy-mm-dd)
tF	Sample last date (yyyy-mm-dd)
Economies	string-vector containing the names of the economies which are part of the economic system
N	Number of country-specific spanned factor (scalar)

FactorLabels	String-list based which contains the labels of all the variables present in the model
ModelType	String-vector containing the label of the model to be estimated
DataFrequency	Character-based-vector. Available options are: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually"
W_type	Three possibilities: <ul style="list-style-type: none"> • "Full Sample": if one wishes ALL weight matrices of each year from which data is available (it may extrapolate the sample period); • "Sample Mean": if one wishes a SINGLE weight matrix containing the average of weights over of the entire sample period; • Some year in particular (e.g. "1998", "2005" ...).
t_First_Wgvar	Sample starting date (year)
t_Last_Wgvar	Sample last date (year)
DataPathMacro	Path of the Excel file conating the macroeconomic data (if any). The default is linked to the excel file present in the package.
DataPathYields	Path of the Excel file conating the yields data (if any). The default is linked to the excel file present in the package.
DataPathTrade	Path of the Excel file conating the trade data (if any). The default is linked to the excel file present in the package.

Value

A list containing the

1. time series of the complete set of bond yields (matrix, JxT or CJxT);
2. time series of the complete set risk factors (matrix, KxT);
3. 'GVARFactors': list of all variables that are used in the estimation of the VARX (see e.g. 'CM_Factors_GVAR' file). If the estimated model type is not GVAR-based, then returns NULL.

Examples

```

DomVar <- c("Eco_Act", "Inflation")
GlobalVar <- c("GBC", "CPI_OECD")
t0 <- "2006-09-01"
tF <- "2019-01-01"
Economies <- c("China", "Brazil", "Mexico", "Uruguay", "Russia")
N <- 2
ModelType <- "JPS"
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)
DataFrequency <- "Monthly"

DataModel <- DataForEstimation(t0, tF, Economies, N, FactorLabels, ModelType, DataFrequency)

```

FactorsGVAR

*Data: Risk Factors for the GVAR - Candelon and Moura (2021)***Description**

Risk factors data used in the GVAR models - Candelon and Moura (2021)

Usage

```
data("CM_Factors_GVAR")
```

Format

list containing the variables used in the GVAR models

References

Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".

ForecastYields

*Gather bond yields forecasts for all the model types***Description**

Gather bond yields forecasts for all the model types

Usage

```
ForecastYields(
  ModelType,
  ModelPara,
  InputsForOutputs,
  FactorLabels,
  Economies,
  DataFrequency,
  JLLinputs,
  GVARinputs,
  BRWinputs
)
```

Arguments

ModelType	a string-vector containing the label of the model to be estimated
ModelPara	List of model parameter estimates (See the "Optimization" function)
InputsForOutputs	list conataining the desired horizon of analysis for the IRFs, GIRFs, FEVDS, and GFEVDs
FactorLabels	a string-list based which contains all the labels of all the variables present in the model
Economies	string-vector containing the names of the economies which are part of the economic system
DataFrequency	text: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually"
JLLinputs	list of necessary inputs for the estimation of JLL-based models (see "JLL" function)
GVARinputs	list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function)
BRWinputs	list of necessary inputs for performing the bias-corrected estimation (see "Bias_Correc_VAR" function)

Value

List containg the following elements

1. Out-of-sample forecasts of bond yields per forecast horizon
2. Out-of-sample forecast errors of bond yields per forecast horizon
3. Root mean square errors per forecast horizon

Examples

```
# See examples in the vignette file of this package (Section 4).
```

Functionf

Set up the vector-valued objective function (Point estimate)

Description

Set up the vector-valued objective function (Point estimate)

Usage

```
Functionf(MLEinputs, Economies, mat, DataFrequency, FactorLabels, ModelType)
```

Arguments

MLEinputs	Set of inputs that are necessary to the log-likelihood function
Economies	string-vector containing the names of the economies which are part of the economic system
mat	vector of maturities (in years) of yields used in estimation ($J \times 1$)
DataFrequency	character-based vector: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually"
FactorLabels	string-list based which contains the labels of all the variables present in the model
ModelType	string-vector containing the label of the model to be estimated

Value

objective function

Examples

```
# See examples in the vignette file of this package (Section 4).
```

GVAR

Estimate a GVAR(1) and a VARX(1,1,1)

Description

Estimate a GVAR(1) and a VARX(1,1,1)

Usage

```
GVAR(GVARinputs, N)
```

Arguments

GVARinputs	List containing the following necessary inputs for the estimation of the GVAR:
	1. Economies: string-vector containing the names of the economies which are part of the economic system
	2. 'GVARFactors': list of all variables that are used in the estimation of the VARX (see e.g. 'CM_Factors_GVAR' file);
	3. 'VARXtype': character-vector containing three possibilities:
	• 'unconstrained': model is estimated without any constrained (each equation is estimated individually by OLS);
	• 'constrained': Spanned Factors': model is estimated taking into account the fact that foreign-pricing-factors do NOT impinge on (i) domestic economic variables and (ii) domestic pricing factors. (equations are estimated by restricted least squares)

- 'constrained': extended by the name of the risk factor: model is estimated taking into account the fact that the restricted factor is only affected by its own lagged values and the lagged values of its own star variables. (equations are estimated by restricted least squares)
4. 'Wgvar': GVAR transition matrix ($C \times C$) - see the output from 'Transition_Matrix' function
- | | |
|---|---|
| N | number of country-specific spanned factors (scalar) |
|---|---|

Value

A list containing

1. parameters of the country-specific VARX(1,1,1)
 - intercept ($M+N \times 1$);
 - phi_1 ($M+N \times M+N$);
 - phi_1^star ($M+N \times M+N$);
 - phi_g ($M+N \times M+N$);
 - Sigma ($M+N \times G$)
2. parameters of the GVAR.
 - F0 ($F \times 1$);
 - F1 ($F \times F$);
 - Sigma_y ($F \times F$)

References

Chudik and Pesaran, (2016). "Theory and Practice of GVAR modelling" (Journal of Economic Surveys)

Examples

```

data(CM_Factors_GVAR)

N <- 3

GVARinputs <- list()
GVARinputs$Economies <- c("China", "Brazil", "Mexico", "Uruguay")
GVARinputs$GVARFactors <- FactorsGVAR
GVARinputs$VARXtype <- "unconstrained"
GVARinputs$Wgvar <- matrix( c(0, 0.83, 0.86, 0.38,
                                0.65, 0, 0.13, 0.55,
                                0.32, 0.12, 0, 0.07,
                                0.03, 0.05, 0.01, 0), nrow = 4, ncol = 4)

GVAR(GVARinputs, N)

```

GVARFactors

*Data: Risk Factors for the GVAR - Candelon and Moura (2023)***Description**

Risk factors data used in the GVAR models - Candelon and Moura (2023)

Usage

```
data("CM_Factors_GVAR_2023")
```

Format

list containing the variables used in the GVAR models

References

Candelon, B. and Moura, R. "Sovereign yield curves and the COVID-19 in emerging markets".

InputsForMLEdensity

Generates several inputs that are necessary to build the likelihood function

Description

Generates several inputs that are necessary to build the likelihood function

Usage

```
InputsForMLEdensity(
  ModelType,
  Yields,
  PdynamicsFactors,
  FactorLabels,
  mat,
  Economies,
  DataFrequency,
  JLLinputs = NULL,
  GVARinputs = NULL,
  BRWinputs = NULL
)
```

Arguments

ModelType	string-vector containing the label of the model to be estimated
Yields	time series of yields (JxT or CJ x T)
PdynamicsFactors	time series of the risk factors (K x T)
FactorLabels	string-list based which contains the labels of all variables present in the model
mat	vector of maturities (in years) used in the estimation
Economies	string-vector containing the names of the economies of the system. If the ModelType selected is "JPS", "JPS jointP", "GVAR sepQ", then only one economy can be selected. For the other models, more than one economy must be selected.
DataFrequency	character-based-vector. Available options are: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually"
JLLinputs	list of necessary inputs for the estimation of JLL-based models (see "JLL" function)
GVARinputs	list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function)
BRWinputs	list of necessary inputs for performing the bias-corrected estimation (see "Bias_Correc_VAR" function)

Details

To ensure that the risk factors matrix is correctly built for the model "JPS", the global factors should be allocated on the first G rows of this matrix.

Value

List of necessary inputs for constructing the model's log-likelihood function

Examples

```
# Example 1:
data(CM_Factors)
data(CM_Yields)

ModelType <- "JPS"
Economies <- "Mexico"
Factors <- RiskFactors
N <- 3
GlobalVar <- c("GBC", "CPI_OECD") # Global Variables
DomVar <- c("Eco_Act", "Inflation") # Domestic Variables
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)

mat <- c(0.25, 0.5, 1, 3, 5, 10)
DataFrequency <- "Monthly"
```



```

} else {
    message("skipping functionality due to missing Suggested dependency")
}

```

InputsForOutputs	<i>Collect the inputs that are used to construct the numerical and the graphical outputs</i>
------------------	--

Description

Collect the inputs that are used to construct the numerical and the graphical outputs

Usage

```

InputsForOutputs(
    ModelType,
    Horiz,
    ListOutputWished,
    OutputLabel,
    WishStationarityQ,
    UnitYields,
    WishGraphYields = 0,
    WishGraphRiskFactors = 0,
    WishOrthoJLLgraphs = 0,
    WishForwardPremia = 0,
    LimFP = NULL,
    WishBootstrap = 0,
    ListBoot = NULL,
    WishForecast = 0,
    ListForecast = NULL
)

```

Arguments

ModelType	String-vector containing the label of the model to be estimated
Horiz	Single numerical vector conataining the desired horizon of analysis for the outputs
ListOutputWished	List of desired graphical outputs. Available options are: "Fit", "IRF", "FEVD", "GIRF", "GFEVD".
OutputLabel	Name of the output label to be stored
WishStationarityQ	User must set 1 if she whishes to impose the largest eigenvalue under the Q to be strictly smaller than 1, otherwise set 0.

UnitYields	(i) "Month": if maturity of yields are expressed in months or (ii) "Year": if maturity of yields are expressed in years
WishGraphYields	Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0".
WishGraphRiskFactors	Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0".
WishOrthoJLLgraphs	Binary variable: set 1, if the user wishes orthogonalized JLL-based graphs to be generated; or set 0, otherwise. Default is set as "0"
WishForwardPremia	Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0".
LimFP	Numerical vector containing the maturities associated with the starting and the ending date of the loan
WishBootstrap	Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0".
ListBoot	List containing the four following elements: <ol style="list-style-type: none"> 1. "methodBS": Desired bootstrap method among (a) 'bs' (standard residual bootstrap), (b) 'wild' (wild bootstrap), (c) 'block' (block bootstrap); 2. "BlockLength": if block bootstrap is chosen, then the user has to specify the lenght of the block (single numerical vector); 3. "ndraws": number of draws; 4. "pctg": level of confidence (single numerical vector expressed in basis points)
WishForecast	Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0".
ListForecast	list containing the three following elements: <ol style="list-style-type: none"> 1. "ForHoriz": forecast horizon; 2. "t0Sample": index of the first variable of the information set; 3. "t0Forecast": index of the first forecast cut-off date.

Value

List of necessary inputs to generate the graphs of the outputs of the desired model

Examples

```
ModelType <- "JPS"
Horiz <- 100
DesiredOutputGraphs <- c("Fit", "GIRF", "GFEVD")
OutputLabel <- "Test"
WishStationarityQ <- 1
WishGraphRiskFac <- 0
```

```

WishGraphYields <- 1

InputsList <- InputsForOutputs(ModelType, Horiz, DesiredOutputGraphs, OutputLabel,
                                WishStationarityQ, WishGraphYields, WishGraphRiskFac)

```

JLL	<i>Set of inputs present at JLL's P-dynamics</i>
-----	--

Description

Set of inputs present at JLL's P-dynamics

Usage

```
JLL(NonOrthoFactors, N, JLLinputs)
```

Arguments

NonOrthoFactors	Risk factors before the orthogonalization (FxT)
N	Number of country-specific spanned factors
JLLinputs	List of necessary inputs to estimate JLL outputs: <ol style="list-style-type: none"> 1. Economies: set of economies that are part of the economic system (string-vector) 2. "DomUnit": name of the economy which is assigned as the dominant unit. If no dominant unit is assigned, then this variable is defined as "None" 3. WishSigmas: equal to "1" if one wishes the variance-covariance matrices and the Cholesky factorizations (can take long if they need to be estimated). Set "0", otherwise. 4. SigmaNonOrtho: NULL or some F x F matrix from the non-orthogonalized dynamics 5. JLLModelType: available options are "JLL original", "JLL jointSigma" or "JLL NoDomUnit"

Details

For the models 'JLL original' or "JLL jointSigma" the name of one dominant economy must be assigned.

For the model 'JLL NoDomUnit', the name of one dominant economy must be set as "None".

Value

List of model parameters from both the orthogonalized and non-orthogonalized versions of the JLL's based models

References

Jotiskhatira, Le and Lundblad (2015). "Why do interest rates in different currencies co-move?" (Journal of Financial Economics)

Examples

```
data(CM_Factors)
ZZ <- RiskFactors
N <- 3

JLLinputs <- list()
JLLinputs$Economies <- c( "China", "Brazil", "Mexico", "Uruguay")
JLLinputs$DomUnit <- "China"
JLLinputs$WishSigmas <- 1
JLLinputs$SigmaNonOrtho <- NULL
JLLinputs$JLLModelType <- "JLL original"

JLL(ZZ, N, JLLinputs)
```

K1XQStationary *Impose stationarity under the Q-measure*

Description

Impose stationarity under the Q-measure

Usage

```
K1XQStationary(StationaryEigenvalues)
```

Arguments

StationaryEigenvalues

Binary variable: set "1" if the user whishes the largest eigenvalue to be strictly smaller than 1. Set "0", otherwise

Value

list

Examples

```
stat <- 1 # Takes values 1 and 0
K1XQStationary(stat)
```

LabFac	<i>Generates the labels factors</i>
--------	-------------------------------------

Description

Generates the labels factors

Usage

```
LabFac(N, DomVar, GlobalVar, Economies, ModelType)
```

Arguments

N	number of spanned factors per country (scalar)
DomVar	character-vector containing the names of the domestic variables
GlobalVar	character-vector containing the names of the global variables
Economies	string-vector containing the names of the economies which are part of the economic system
ModelType	string-vector containing the label of the model to be estimated

Value

List containing the country-specific risk factor labels

Examples

```
N <- 2
DomVar <- c("inflation", "Economic growth")
GlobalVar <- "Commodity Prices"
Economies <- c("U.S.", "Canada", "Germany", "Japan")
ModelType <- "JPS"

VarLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)
```

ListModelInputs	<i>Concatenate the model-specific inputs in a list</i>
-----------------	--

Description

Concatenate the model-specific inputs in a list

Usage

```
ListModelInputs(
  ModelType,
  Data = NULL,
  Economies,
  VARXtype = NULL,
  t_First_Wgvar = NULL,
  t_Last_Wgvar = NULL,
  W_type = NULL,
  DomUnit = NULL,
  WishSigmas = NULL,
  SigmaNonOrtho = NULL,
  BiasCorrection = 0,
  flag_mean = NULL,
  gamma = NULL,
  N_iter = NULL,
  N_burn = NULL,
  B = NULL,
  checkBRW = NULL,
  B_check = NULL,
  DataPathTrade = NULL
)
```

Arguments

ModelType	string-vector containing the label of the model to be estimated
Data	dataset generated from the "DataForEstimation" function
Economies	string-vector containing the names of the economies of the system
VARXtype	string-vector containing the VARX feature (see "GVAR" function) (GVAR-based models)
t_First_Wgvar	Sample starting date (year) (GVAR-based models)
t_Last_Wgvar	Sample last date (year) (GVAR-based models)
W_type	Criterion used in the computation of the star variables (see "Transition_Matrix" function) (GVAR-based models)
DomUnit	name of the economy which is assigned as the dominant unit (JLL-based models)
WishSigmas	equal to "1" if one wishes the variance-covariance matrices and the Cholesky factorizations (JLL-based models)
SigmaNonOrtho	NULL or some F x F matrix from the non-orthogonalized dynamics (JLL-based models)
BiasCorrection	binary variable. it takes value equal to 1 if the user whishes the estimates to be bias-corrected and 0, otherwise. (BRW model)
flag_mean	flag whether mean- (TRUE) or median- (FALSE) unbiased estimation is desired
gamma	adjustment parameter (BRW model)

N_iter	number of iterations (BRW model)
N_burn	number of burn-in iterations (BRW model)
B	number of bootstrap samples (BRW model)
checkBRW	flag whether the user wishes to perform the closeness check (BRW model)
B_check	number of bootstrap samples for closeness check
DataPathTrade	path of the Excel file containing the data (if any)

Examples

```
ModelType <- "JLL original"
Eco <- c("China", "Brazil", "Mexico", "Uruguay")
DU <- "China"
Sig <- 1
NonOrtho <- 0
```

```
ListModelInputs(ModelType, Economies = Eco, DomUnit = DU, WishSigmas = Sig, SigmaNonOrtho = NonOrtho)
```

Maturities	<i>Create a vector of numerical maturities in years</i>
------------	---

Description

Create a vector of numerical maturities in years

Usage

```
Maturities(DataYields, Economies, UnitYields)
```

Arguments

DataYields	matrix containing all yields of the system (JxT, if the model is single-country-based or CJxT if the model is multi-country-based)
Economies	vector containing names of all the economies of the system
UnitYields	(i) "Month": if maturity of yields are expressed in months or (ii) "Year": if maturity of yields are expressed in years

Value

Vector containing all observed maturities expressed in years

Examples

```
data('CM_Yields')
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
Maturities(Yields, Economies, "Month")
```

ModelPara

*Replications of the JPS (2014) outputs by the MultiATSM package***Description**

Unspanned macro risk model outputs by the MultiATSM package

Usage

```
data("JPSrep")
```

Format

list of inputs and outputs

inputs general model inputs

ests model parameters estimates (JPS form)

llk log-likelihood of the observations

rot model parameters estimates (rotation form)

MultiATSM

*ATSM Package***Description**

Estimation of several classes of affine term structure of interest rates models.

Author(s)

Rubens Moura <rubens.gtmoura@gmail.com>

NumOutputs	<i>Construct the model numerical outputs (model fit, IRFs, GIRFs, FEVDs, GFEVDs, and risk premia decomposition)</i>
------------	---

Description

Construct the model numerical outputs (model fit, IRFs, GIRFs, FEVDs, GFEVDs, and risk premia decomposition)

Usage

```
NumOutputs(ModelType, ModelPara, InputsForOutputs, FactorLabels, Economies)
```

Arguments

ModelType	a string-vector containing the label of the model to be estimated
ModelPara	List of model parameter estimates (See the "Optimization" function)
InputsForOutputs	list conataining the desired horizon of analysis for the model fit, IRFs, GIRFs, FEVDs, GFEVDs and risk premia decomposition
FactorLabels	a string-list based which contains all the labels of all the variables present in the model
Economies	a string-vector containing the names of the economies which are part of the economic system

Value

List of the model numerical outputs, namely

1. Model fit of bond yields
2. IRFs
3. FEVDs
4. GIRFs
5. GFEVDs
6. Risk premia decomposition

Examples

```
# See examples in the vignette file of this package (Section 4).
```

Optimization	<i>Peform the minimization of mean(f)</i>
--------------	---

Description

Peform the minimization of $\text{mean}(f)$

Usage

```
Optimization(
  f,
  tol,
  varargin,
  FactorLabels,
  Economies,
  ModelType,
  JLLinputs = NULL,
  GVARinputs = NULL
)
```

Arguments

<code>f</code>	vector-valued objective function (function)
<code>tol</code>	convergence tolerance (scalar). For ML estimation, a reasonable value is <code>tol <- 1e-4</code>
<code>varargin</code>	list containg starting values and constraints: for each input argument K (of f), we need four inputs that look like: <ol style="list-style-type: none"> 1. a starting value: <code>K0</code> 2. a variable label ('<code>K0</code>') followed by a ':' followed by a type of constraint. The constraint can be: <ul style="list-style-type: none"> • 'bounded': bounded matrix; • 'Jordan' or 'Jordan MultiCountry': a matrix of Jordan type; • 'psd': psd matrix; • 'stationary': largest eigenvalue of the risk-neutral feedback matrix is strictly smaller than 1; • 'diag' or 'BlockDiag': a diagonal or block diagonal matrix. • 'JLLstructure': to impose the zero-restrictions on the variance-variance matrix along the lines of the JLL models 3. a lower bound <code>lb</code> (<code>lb <- NULL</code> -> no lower bound) 4. an upper bound <code>ub</code> (<code>ub <- NULL</code> -> no upper bound) 5. Specification of the optimization settings: <ul style="list-style-type: none"> • 'iter off': hide the printouts of the numerical optimization routines; • 'fminunc only': only uses fminunc for the optimization; • "fminsearch only": only uses fminsearch for the optimization.

FactorLabels	string-list based which contains the labels of all the variables present in the model
Economies	string-vector containing the names of the economies which are part of the economic system
ModelType	string-vector containing the label of the model to be estimated
JLLinputs	inputs used in the estimation of the JLL-based models; Default is set to NULL
GVARinputs	inputs used in the estimation of the GVAR-based models; Default is set to NULL

Details

If a variable name starts with a '@', it means that that parameter will be analytically concentrated out in the specification of f. In this case, no starting value is needed for this particular parameter (an empty matrix can be provided as a starting value).

Value

- (i) out: list of second output produced by f (the first output of f must be the objective value to be minimized).
- (ii) x: list containing parameter estimates

References

This function is based on the "LS_opt" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

Examples

```
#' # See examples in the vignette file of this package (Section 4).
```

ParaLabels

Create the variable labels used in the estimation

Description

Create the variable labels used in the estimation

Usage

```
ParaLabels(ModelType, WishStationarityQ)
```

Arguments

ModelType	a string-vector containing the label of the model to be estimated
WishStationarityQ	User must set "1" if she whishes to impose the largest eigenvalue under the Q to be strictly smaller than 1. Otherwise set "0"

Value

list containing the features of the parameters that will be used in the estimation

Examples

```
ModelType <- "GVAR jointQ"
WishStationarityQ <- 1
ParaLabels(ModelType, WishStationarityQ)
```

pca_weights_one_country

Weigth matrix from principal components (matrix of eigenvectors)

Description

Weigth matrix from principal components (matrix of eigenvectors)

Usage

```
pca_weights_one_country(Y, Economy)
```

Arguments

Y	matrix dimension (J x T), where J - the number of maturities and T - time series length
Economy	string-vector containg the name of one economy

Value

matrix (J x J)

Examples

```
data("CM_Yields")
pca_weights_one_country(Yields, Economy= "Brazil")
```

Reg_K1Q	<i>Estimate the risk-neutral feedback matrix K1Q using linear regressions</i>
---------	---

Description

Estimate the risk-neutral feedback matrix K1Q using linear regressions

Usage

```
Reg_K1Q(Y, mat, Z, dt, type)
```

Arguments

Y	matrix of yields used in estimation (J x T)
mat	vector of maturities (in years) of yields used in estimation (J x 1)
Z	pricing factors (can be yields-based or non-yields/macro variables) (N x T)
dt	time unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1.
type	'Jordan' -> K1Q will be of the Jordan type

Value

Risk neutral feedback matrix K1Q.

References

This function is based on the "Reg_K1Q" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

Examples

```
data(CM_Yields)

Y_China <- Yields[1:6,]
Z_China <- Spanned_Factors(Y_China, Economies ="China", N=3)
mat <- c(0.25 , 0.5 , 1, 3, 5, 10)
dt <- 1/12
type <- 'Jordan'
Reg_K1Q(Y_China, mat, Z_China, dt, type)
```

RiskFactors*Data: Risk Factors - Candelon and Moura (2021)***Description**

Risk factors data used in Candelon and Moura (2021)
 Risk factors data used in Candelon and Moura (2023)

Usage

```
data("CM_Factors")
data("CM_Factors_2023")
```

Format

matrix containing the risk factors of the models
 matrix containing the risk factors of the models

References

Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".
 Candelon, B. and Moura, R. "Sovereign yield curves and the COVID-19 in emerging markets".

RMSEsep*Compute the root mean square error ("sep Q" models)***Description**

Compute the root mean square error ("sep Q" models)

Usage

```
RMSEsep(ForecastOutputs)
```

Arguments

ForecastOutputs
 List of country-specific forecasts (see "ForecastYieldsSepQ" function)

Spanned_Factors	<i>Compute the country-specific spanned factors</i>
-----------------	---

Description

Compute the country-specific spanned factors

Usage

```
Spanned_Factors(Yields, Economies, N)
```

Arguments

Yields	matrix (J x T), where J - the number of maturities and T - time series length
Economies	C-dimensional string-vector containing the names of the economies which are part of the economic system
N	scalar: desired number of spanned factors (maximum number allowed is N= J)

Value

Matrix containing the N spanned for all the countries of the system (CJ xT)

Examples

```
data(CM_Yields)
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
N <- 3
Spanned_Factors(Yields, Economies, N)
```

StarFactors	<i>Generates the star variables necessary for the GVAR estimation</i>
-------------	---

Description

Generates the star variables necessary for the GVAR estimation

Usage

```
StarFactors(RiskFactors, Economies, W)
```

Arguments

RiskFactors	time series of the risk factors (F x T)
Economies	string-vector containing the names of the economies which are part of the economic system
W	GVAR transition matrix (C x C)

Value

List containg the star factors of each country of the economic system

Examples

```
data(CM_Factors)
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
Wgvar <- matrix( c(0, 0.83, 0.86, 0.38, 0.65, 0, 0.13, 0.55,
                  0.32, 0.12, 0, 0.07, 0.03, 0.05, 0.01, 0), nrow = 4, ncol = 4)
rownames(Wgvar) <- Economies
colnames(Wgvar) <- Economies
StarFactors(RiskFactors, Economies, Wgvar)
```

TradeFlows

*Data: Trade Flows - Candelon and Moura (2021)***Description**

Trade Flows data used in Candelon and Moura (2021)

Usage

```
data("CM_Trade")
```

Format

list containing the bilateral trade flows

References

Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".

Trade_Flows

*Data: Trade Flows - Candelon and Moura (2023)***Description**

Trade Flows data used in Candelon and Moura (2023)

Usage

```
data("CM_Trade")
```

Format

list containing the bilateral trade flows

References

Candelon, B. and Moura, R. "Sovereign yield curves and the COVID-19 in emerging markets".

Transition_Matrix	<i>Compute the transition matrix required in the estimation of the GVAR model</i>
-------------------	---

Description

Compute the transition matrix required in the estimation of the GVAR model

Usage

```
Transition_Matrix(
  t_First,
  t_Last,
  Economies,
  type,
  DataPath = NULL,
  Data = NULL
)
```

Arguments

t_First	Sample starting date (year)
t_Last	Sample last date (year)
Economies	Vector containing the names of all the economies of the system.
type	Three possibilities: <ul style="list-style-type: none"> • "Full Sample": if one wishes ALL weight matrices of each year from which data is available (it may extrapolate the sample period); • "Sample Mean": if one wishes a SINGLE weight matrix containing the average of weights over of the entire sample period; • Some year in particular (e.g. "1998", "2005" ...).
DataPath	path of the Excel file containing the data (if any). The default is linked to the Excel file available in the package.
Data	Data for computing the transition matrix. Default is set to NULL.

Details

NOTE: if there is missing data for any country of the system for that particularly year, then the transition matrix will include only NAs.

Value

matrix or list of matrices

Examples

```
data(CM_Trade)

t_First <- "2006"
t_Last <- "2019"
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
type <- "Sample Mean"
Transition_Matrix(t_First, t_Last, Economies, DataPath = NULL, Data = TradeFlows)
```

VAR

Estimates a VAR(1)

Description

Estimates a VAR(1)

Usage

```
VAR(RiskFactors, VARtype, Bcon = NULL)
```

Arguments

RiskFactors	matrix containing all the risk factors (K x T)
VARtype	string-vector which accommodates two possibilities: 'unconstrained' or 'constrained'
Bcon	constraints matrix (K+1 x N) - should contain an intercept. IfBcon(i,j) = nan → B(i,j) is a free parameter. Default is set to NULL.

Value

intercept, feedback matrix and the variance-covariance matrix of a VAR(1)

Examples

```
data("CM_Factors")
#Example 1
VAR(RiskFactors, VARtype= 'unconstrained')
#Example 2
K <- nrow(RiskFactors)
Bcon <-matrix(0, nrow = K, ncol = K+1)
Bcon[,1:3] <- NaN
```

```
VAR(RiskFactors, VARtype= 'constrained', Bcon)
```

Yields

Data: Yields - Candelon and Moura (2021)

Description

Yields data used in Candelon and Moura (2021)
Bond yield data used in Candelon and Moura (2023)

Usage

```
data("CM_Yields")  
data("CM_Yields_2023")
```

Format

matrix containing the Yields of the models
matrix containing the Yields of the models

References

- Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".
Candelon, B. and Moura, R. "Sovereign yield curves and the COVID-19 in emerging markets".

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