

# Package ‘GaSP’

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**Type** Package

**Title** Train and Apply a Gaussian Stochastic Process Model

**Version** 1.0.6

**Description** Train a Gaussian stochastic process model of an unknown function, possibly observed with error, via maximum likelihood or maximum a posteriori (MAP) estimation, run model diagnostics, and make predictions, following Sacks, J., Welch, W.J., Mitchell, T.J., and Wynn, H.P. (1989) ``Design and Analysis of Computer Experiments'', Statistical Science, <doi:10.1214/ss/1177012413>. Perform sensitivity analysis and visualize low-order effects, following Schonlau, M. and Welch, W.J. (2006), ``Screening the Input Variables to a Computer Model Via Analysis of Variance and Visualization'', <doi:10.1007/0-387-28014-6\_14>.

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borehole	<i>Data for the borehole function</i>
----------	---------------------------------------

---

## Description

Training and test data for the borehole function; see source for background.

## Usage

```
borehole
```

## Format

A list with the following four data frames:

**x** 8-dimensional input for 40 training runs.

**y** Output (the flow) for the 40 training runs in **x**.

**x\_pred** 8-dimensional input for 1000 test runs at which to predict **y**.

**y\_true** Output for the 1000 runs in **x\_pred**.

## Source

<https://www.sfu.ca/~ssurjano/borehole.html>

---

CrossValidate	<i>Cross-validated predictions for a GaSPModel object.</i>
---------------	--

---

**Description**

Compute leave-one-out cross-validated predictions for a GaSPModel object.

**Usage**

```
CrossValidate(GaSP_model)
```

**Arguments**

GaSP\_model      Object of class [GaSPModel](#).

**Value**

A data frame with two columns: the cross-validated predictions Pred and their standard errors SE.

**Note**

[RMSE](#) computes the root mean squared error of the predictions. [PlotPredictions](#) and [PlotResiduals](#) plot the predictions or their residuals; [PlotStdResiduals](#) and [PlotQQ](#) plot the standardized residuals.

**Examples**

```
borehole_cv <- CrossValidate(borehole_fit)
```

---

DescribeX	<i>Describe the input variables.</i>
-----------	--------------------------------------

---

**Description**

Describe the input variables to set up integration or summation ranges for Visualize.

**Usage**

```
DescribeX(  
  x_names,  
  x_min,  
  x_max,  
  support = NULL,  
  num_levels = NULL,  
  distribution = NULL  
)
```

**Arguments**

<code>x_names</code>	A vector of character strings containing the names of the input variables.
<code>x_min, x_max</code>	Vectors of the same length as <code>x_names</code> containing the minima and maxima, respectively, of the input variables.
<code>support</code>	Optional vector of character strings of the same length as <code>x_names</code> . Valid strings for a variable are: "Continuous" (continuous between the input's <code>x_min</code> and <code>x_max</code> ); "Fixed" (the input's <code>x_min</code> must equal its <code>x_max</code> ); and "Grid" (which requires the next argument).
<code>num_levels</code>	An optional vector of integers for the number of levels of each input; must be present if the <code>support</code> argument includes "Grid". An input's number of levels is 0 if it is "Continuous", 1 if it is "Fixed", or > 1 if it is "Grid" to define an equally spaced grid inclusive of the input's <code>x_min</code> and <code>x_max</code> .
<code>distribution</code>	An optional vector of character strings of the same length as <code>x_names</code> to define the weight distributions of the input variables. Valid strings are "Uniform" or "Normal" (ignored for "Fixed" inputs).

**Value**

A data frame with the following columns: `Variable` (containing `x_names`), `Min` (containing `x_min`), and `Max` (containing `x_max`), plus the optional columns `Support` (from `support`), `NumberLevels` (from `num_levels`), and `Distribution` (from `distribution`).

**Note**

Does not check against [GaSPModel](#) and all characters are CASE SENSITIVE.

**Examples**

```
borehole_x_names <- colnames(borehole$x)
borehole_min <- c(0.05, 100.00, 63070.00, 990.00, 63.10, 700.00, 1120.00, 9855.00)
borehole_max <- c(0.15, 50000.00, 115600.00, 1110.00, 116.00, 820.00, 1680.00, 12045.00)
borehole_x_desc <- DescribeX(borehole_x_names, borehole_min, borehole_max)
```

---

 Fit

*Fit a GaSP model.*


---

**Description**

Fit (train) a GaSP model.

**Usage**

```
Fit(
  x,
  y,
  reg_model,
  sp_model = NULL,
  cor_family = c("PowerExponential", "Matern"),
  cor_par = data.frame(0),
  random_error = c(FALSE, TRUE),
  sp_var = -1,
  error_var = -1,
  nugget = 1e-09,
  tries = 10,
  seed = 500,
  fit_objective = c("Likelihood", "Posterior"),
  theta_standardized_min = 0,
  theta_standardized_max = .Machine$double.xmax,
  alpha_min = 0,
  alpha_max = 1,
  derivatives_min = 0,
  derivatives_max = 3,
  log_obj_tol = 1e-05,
  log_obj_diff = 0,
  lambda_prior = 0.1,
  model_comparison = c("Objective", "CV")
)
```

**Arguments**

<code>x</code>	A data frame containing the input (explanatory variable) training data.
<code>y</code>	A vector or a data frame with one column containing the output (response) training data.
<code>reg_model</code>	The regression model, specified as a formula, but note the left-hand side of the formula is unused; see example.
<code>sp_model</code>	An optional stochastic process model, specified as a formula, but note the left-hand side of the formula and the intercept are unused. The default NULL uses all column names in <code>x</code> .
<code>cor_family</code>	A character string specifying the (product, anisotropic) correlation-function family: "PowerExponential" for the power-exponential family or "Matern" for the Matern family.
<code>cor_par</code>	An optional data frame containing the correlation parameters with one row per <code>sp_model</code> term and two columns set up as described in <a href="#">GaSPModel</a> Details; only used to start the first objective optimization (see Details).
<code>random_error</code>	A boolean for the presence or not of a random (measurement, white-noise) error term.

sp_var, error_var	Starting values of the stochastic process and error variances for the first try to optimize the objective (see Details); valid (i.e., nonnegative) values will only be used if random_error = TRUE. The invalid default value of -1 indicates that a starting value will be chosen by Fit.
nugget	For numerical stability the proportion of the total variance due to random error is fixed at this value (random_error = FALSE) or bounded below by it (random_error = TRUE).
tries	Number of optimizations of the objective from different random starting points.
seed	The random-number seed to generate starting points.
fit_objective	The objective that Fit attempts to optimize: "Likelihood" (maximum likelihood estimation) or "Posterior" (Bayesian maximum a posteriori estimation).
theta_standardized_min, theta_standardized_max	The minimum and maximum of the standardized $\theta$ parameter (see Details).
alpha_min, alpha_max	The minimum and maximum of the $\alpha$ parameter of power-exponential.
derivatives_min, derivatives_max	The minimum and maximum of the $\delta$ parameter of Matern.
log_obj_tol	An absolute tolerance for terminating the optimization of the log of the objective.
log_obj_diff	The critical value for the change in the log objective for informal tests during optimization of correlation parameters. No testing is done with the default of 0; a larger critical value such as 2 may give a more parsimonious model.
lambda_prior	The rate parameter of an exponential prior for each $\theta$ parameter; used only if fit_objective = "Posterior".
model_comparison	The criterion used to select from multiple solutions when tries > 1: the objective function ("Objective") or leave-one-out cross validation ("CV").

## Details

Fit numerically optimizes the profile objective function with respect to the correlation parameters; the mean and overall variance parameters are estimated in closed form given the correlation parameters.

A cor\_par data frame supplied by the user is the starting point for the first optimization try. If random\_error = TRUE, then sp\_var / (sp\_var + error\_var) is another correlation parameter to be optimized; sp\_var and error\_var values supplied by the user will initialize this parameter for the first try.

Set random\_error = TRUE to estimate the variance of the random (measurement, white-noise) error; a small nugget error variance is for numerical stability.

For term  $j$  in the stochastic-process model, the estimate of  $\theta_j$  is constrained between theta\_standardized\_min /  $r_j^2$  and theta\_standardized\_max /  $r_j^2$ , where  $r_j$  is the range of term  $j$ . Note that Fit returns unscaled estimates relating to the original, unscaled inputs.

**Value**

A GaSPModel object, which is a list with the following components:

x	The data frame containing the input training data.
y	The training output data, now as a vector.
reg_model	The regression model, now in the form of a data frame.
sp_model	The stochastic process model, now in the form of a data frame.
cor_family	The correlation family.
cor_par	A data frame for the estimated correlation parameters.
random_error	The boolean for the presence or not of a random error term.
sp_var	The estimated stochastic process variance.
error_var	The estimated random error variance.
beta	A data frame holding the estimated regression-model parameters.
objective	The maximum value found for the objective function: the log likelihood (fit_objective = "Likelihood") or the log posterior (fit_objective = "Posterior").
cond_num	The condition number.
CVRMSE	The leave-one-out cross-validation root mean squared error.

**References**

Sacks, J., Welch, W.J., Mitchell, T.J., and Wynn, H.P. (1989) "Design and Analysis of Computer Experiments", *Statistical Science*, 4, pp. 409-423, doi:10.1214/ss/1177012413.

**Examples**

```
x <- borehole$x
y <- borehole$y
borehole_fit <- Fit(
  reg_model = ~1, x = x, y = y, cor_family = "Matern",
  random_error = FALSE, nugget = 0, fit_objective = "Posterior"
)
```

---

GaSPModel

---

*Create a GaSPModel object.*


---

**Description**

Return a template for a GaSPModel object.

**Usage**

```

GaSPModel(
  x,
  y,
  reg_model,
  sp_model = NULL,
  cor_family = c("PowerExponential", "Matern"),
  cor_par,
  random_error = c(FALSE, TRUE),
  sp_var,
  error_var = 0
)

```

**Arguments**

x	A data frame containing the input (explanatory variable) training data.
y	A vector or a data frame with one column containing the output (response) training data.
reg_model	The regression model, specified as a formula, but note the left-hand side of the formula is unused; see example.
sp_model	An optional stochastic process model, specified as a formula, but note the left-hand side of the formula and the intercept are unused. The default NULL uses all column names in x.
cor_family	A character string specifying the (product, anisotropic) correlation-function family: "PowerExponential" for the power-exponential family or "Matern" for the Matern family.
cor_par	A data frame containing the correlation parameters with one row per sp_model term and two columns (see Details).
random_error	A boolean for the presence or not of a random (measurement, white-noise) error term.
sp_var	The stochastic process variance.
error_var	The random error variance, with default 0.

**Details**

The data frame `cor_par` contains one row for each term in the stochastic process model. There are two columns. The first is named `Theta`, and the second is either `Alpha` (power-exponential) or `Derivatives` (Matern). Let  $h_j$  be a distance between points for term  $j$  in the stochastic-process model. For power-exponential, the contribution to the product correlation from term  $j$  depends on a distance-scale parameter  $\theta_j$  from the `Theta` column and a smoothness parameter  $\alpha_j$  from the `Alpha` column; the contribution is  $\exp(-\theta_j h_j^{2-\alpha_j})$ . For example,  $\alpha_j = 0$  gives the squared-exponential (Gaussian) correlation. The contribution to the product correlation for Matern also depends on  $\theta_j$ , and the second parameter is the number of derivatives  $\delta_j = 0, 1, 2, 3$  from the `Derivatives` column. The contribution is  $\exp(-\theta_j h_j)$  for  $\delta_j = 0$  (the exponential correlation),  $\exp(-\theta_j h_j)(\theta_j h_j + 1)$  for  $\delta_j = 1$ ,  $\exp(-\theta_j h_j)((\theta_j h_j)^2/3 + \theta_j h_j + 1)$  for  $\delta_j = 2$ , and  $\exp(-\theta_j h_j^2)$  for  $\delta_j = 3$  (the squared-exponential correlation). Note that  $\delta_j = 3$  codes for a limiting infinite number of derivatives. This



is not the usual parameterization of the Matern, but it is consistent with power-exponential for the exponential and squared-exponential special cases common to both.

A value should be given to `error_var` if the model has a random-error term (`random_error = TRUE`), and a small "nugget" such as  $10^{-9}$  may be needed for improved numerical conditioning.

### Value

A `GaSPModel` object, which is a list with the following components:

<code>x</code>	The data frame containing the input training data.
<code>y</code>	The training output data, now as a vector.
<code>reg_model</code>	The regression model, now in the form of a data frame.
<code>sp_model</code>	The stochastic process model, now in the form of a data frame.
<code>cor_family</code>	The correlation family.
<code>cor_par</code>	The data frame containing the correlation parameters.
<code>random_error</code>	The boolean for the presence or not of a random error term.
<code>sp_var</code>	The stochastic process variance.
<code>error_var</code>	The random error variance.
<code>beta</code>	A placeholder for a data frame to hold the regression-model parameters.
<code>objective</code>	A placeholder for the maximum fit objective.
<code>cond_num</code>	A placeholder for the condition number.
<code>CVRMSE</code>	A placeholder for the model's cross-validated root mean squared error.

### Note

This function does not execute `Fit` and is intended for `CrossValidate`, `Predict` and `Visualize` with models trained otherwise by the user. Placeholders do not need to be specified to execute these further functions, as they are always recomputed as needed.

### References

Sacks, J., Welch, W.J., Mitchell, T.J., and Wynn, H.P. (1989) "Design and Analysis of Computer Experiments", *Statistical Science*, 4, pp. 409-423, doi:10.1214/ss/1177012413.

### Examples

```
x <- borehole$x
y <- borehole$y
theta <- c(
  5.767699e+01, 0.000000e+00, 0.000000e+00, 1.433571e-06,
  0.000000e+00, 2.366557e-06, 1.695619e-07, 2.454376e-09
)
alpha <- c(
  1.110223e-16, 0.000000e+00, 0.000000e+00, 0.000000e+00,
  0.000000e+00, 0.000000e+00, 2.494862e-03, 0.000000e+00
)
cor_par <- data.frame(Theta = theta, Alpha = alpha)
```

```
rownames(cor_par) <- colnames(borehole$x)
sp_var <- 38783.7
borehole_gasp <- GaSPModel(
  x = borehole$x, y = borehole$y,
  reg_model = ~1, cor_family = "PowerExponential",
  cor_par = cor_par, random_error = FALSE,
  sp_var = sp_var
)
```

---

PlotAll	<i>Execute</i> PlotPredictions, PlotResiduals, PlotStdResiduals, PlotMainEffects, and PlotJointEffects.
---------	---

---

### Description

Execute PlotPredictions, PlotResiduals and PlotStdResiduals (all applied to cross validation only), PlotMainEffects, and PlotJointEffects.

### Usage

```
PlotAll(
  GaSP_model,
  cross_validation,
  visualization,
  y_name = "y",
  y_units = "",
  x_units = NULL,
  se_plot = TRUE,
  y_values = NULL,
  se_values = NULL,
  pch = 1
)
```

### Arguments

GaSP_model	Object of class <a href="#">GaSPModel</a> , the entire model will be verified but only x and y will be used.
cross_validation	A data frame returned by <a href="#">CrossValidate</a> .
visualization	A list object returned by <a href="#">Visualize</a> .
y_name	An optional character string containing the output variable name (for labels).
y_units	An optional character string containing the units of the output variable (for labels).
x_units	An optional vector of character strings containing the units of the input variables (for labels).
se_plot	An optional boolean indicating whether to make standard-error contour plots.

y_values	An optional vector of contour values for the estimated joint effects.
se_values	An optional vector of contour values for the standard errors.
pch	Plotting symbol for plot; default is open circle.

**Value**

No return value, generates plots.

**Examples**

```
PlotAll(borehole_fit, borehole_cv, borehole_vis)
```

---

PlotJointEffects	<i>Plot the estimated joint effects.</i>
------------------	--

---

**Description**

Plot the estimated joint effects.

**Usage**

```
PlotJointEffects(
  joint_effect,
  anova_percent,
  x_units = NULL,
  y_name = "y",
  y_units = "",
  se_plot = TRUE,
  y_values = NULL,
  se_values = NULL
)
```

**Arguments**

joint_effect	A data frame from <a href="#">Visualize</a> with plotting coordinates for the estimated joint effects.
anova_percent	A data frame from <a href="#">Visualize</a> of ANOVA percentages.
x_units	An optional vector of character strings containing the units of the input variables (for labels).
y_name	An optional character string containing the output variable name (for labels).
y_units	An optional character string containing the units of the output variable (for labels).
se_plot	An optional boolean indicating whether to make standard-error contour plots.
y_values	An optional vector of contour values for the estimated joint effects.
se_values	An optional vector of contour values for the standard errors.

**Details**

Plots are sent to the active device.

**Value**

No return value, generates plots.

**Examples**

```
PlotJointEffects(borehole_vis$joint_effect, borehole_vis$anova_percent)
```

---

PlotMainEffects	<i>Plot the estimated main effects.</i>
-----------------	---

---

**Description**

Plot the estimated main effects.

**Usage**

```
PlotMainEffects(
  main_effect,
  anova_percent,
  x_units = NULL,
  y_name = "y",
  y_units = ""
)
```

**Arguments**

main_effect	A data frame from <a href="#">Visualize</a> with plotting coordinates for the estimated main effects.
anova_percent	A data frame from <a href="#">Visualize</a> of ANOVA percentages.
x_units	An optional vector of character strings containing the units of the input variables (for labels).
y_name	An optional character string containing the output variable name (for labels).
y_units	An optional character string containing the units of the output variable (for labels).

**Details**

Plots are sent to the active device. Each plot shows an estimated main effect (red solid line) and pointwise approximate 95% confidence limits (green dashed line).

**Value**

No return value, generates plots.

**Examples**

```
PlotMainEffects(borehole_vis$main_effect, borehole_vis$anova_percent)
```

---

PlotPredictions	<i>Plot true versus predicted output.</i>
-----------------	---

---

**Description**

Plot true versus predicted output (response) made by Predict or CrossValidate.

**Usage**

```
PlotPredictions(
  y_pred,
  y,
  y_name = "y",
  y_units = "",
  title = c("Predict", "CrossValidate"),
  pch = 1
)
```

**Arguments**

y_pred	A data frame of predicted output values made by Predict or CrossValidate.
y	A vector of length equal to the number of rows in y_pred containing the true output values.
y_name	An optional character string containing the output variable name (for labels).
y_units	An optional character string constaining the units of the output variable (for labels).
title	A character string for the name of the function generating the predictions (for an appropriate title): "Predict" from <a href="#">Predict</a> or "CrossValidate" from <a href="#">CrossValidate</a> ; "" for no title.
pch	Plotting symbol for plot; default is open circle.

**Value**

No return value, generates plots.

**Examples**

```
PlotPredictions(borehole_cv, y, title = "CrossValidate")
```

```
PlotPredictions(borehole_pred$y_pred, borehole$y_true, title = "Predict")
```

---

PlotQQ	<i>Normal quantile-quantile (Q-Q) plot.</i>
--------	---

---

**Description**

Normal quantile-quantile (Q-Q) plot of the standardized residuals of predictions from Predict or CrossValidate.

**Usage**

```
PlotQQ(y_pred, y, y_name = "y")
```

**Arguments**

y_pred	A data frame of predicted output values made by Predict or CrossValidate.
y	A vector of length equal to the number of rows in y_pred containing the true output values.
y_name	An optional character string containing the output variable name (for labels).

**Value**

No return value, generates plots.

**Examples**

```
PlotQQ(borehole_cv, y)
```

---

PlotResiduals	<i>Plot residuals versus each input variable.</i>
---------------	---

---

**Description**

Plot residuals versus each input variable.

**Usage**

```
PlotResiduals(  
  x,  
  y_pred,  
  y,  
  x_units = NULL,  
  y_name = "y",  
  y_units = "",  
  pch = 1  
)
```

**Arguments**

x	A data frame with number of rows equal to the number of rows in y_pred containing the input (explanatory) variables.
y_pred	A data frame of predicted output values made by Predict or CrossValidate.
y	A vector of length equal to the number of rows in y_pred containing the true output values.
x_units	An optional vector of character strings containing the units of the input variables in x (for labels).
y_name	An optional character string containing the output variable name (for labels).
y_units	An optional character string containing the units of the output variable (for labels).
pch	Plotting symbol for plot; default is open circle.

**Value**

No return value, generates plots.

**Examples**

```
PlotResiduals(x, borehole_cv, y)
```

---

PlotStdResiduals      *Plot standardized residuals versus predictions.*

---

**Description**

Plot standardized residuals versus predictions made by Predict or CrossValidate.

**Usage**

```
PlotStdResiduals(  
  y_pred,  
  y,  
  y_name = "y",  
  y_units = "",  
  title = c("Predict", "CrossValidate"),  
  pch = 1  
)
```

**Arguments**

<code>y_pred</code>	A data frame of predicted output values made by <code>Predict</code> or <code>CrossValidate</code> .
<code>y</code>	A vector of length equal to the number of rows in <code>y_pred</code> containing the true output values.
<code>y_name</code>	An optional character string containing the output variable name (for labels).
<code>y_units</code>	An optional character string containing the units of the output variable (for labels).
<code>title</code>	A character string for the name of the function generating the predictions (for an appropriate title): "Predict" from <code>Predict</code> or "CrossValidate" from <code>CrossValidate</code> ; "" for no title.
<code>pch</code>	Plotting symbol for plot; default is open circle.

**Value**

No return value, generates plots.

**Examples**

```
PlotStdResiduals(borehole_cv, y, title = "CrossValidate")
```

---

Predict	<i>Predict from a GaSPModel object.</i>
---------	---

---

**Description**

Predict from a `GaSPModel` object.

**Usage**

```
Predict(GaSP_model, x_pred, generate_coefficients = c(FALSE, TRUE))
```

**Arguments**

<code>GaSP_model</code>	Object of class <code>GaSPModel</code> .
<code>x_pred</code>	A data frame containing the values of the input variables at which to predict the output.
<code>generate_coefficients</code>	A boolean indicating whether coefficients for further external predictions are generated.

**Value**

A list with the following elements:

<code>y_pred</code>	A data frame with two columns: the predictions <code>Pred</code> and their standard errors <code>SE</code> .
<code>pred_coefs</code>	A vector of coefficients for further predictions; NULL if <code>generate_coefficients</code> is FALSE.



**Note**

The vector of prediction coefficients in `pred_coeffs` can be used as follows. Let  $c$  denote the coefficients and let  $r$  denote a vector with element  $i$  containing the correlation between the output at a given new point and the output at training point  $i$ . Then the prediction for the output at the new point is the dot product of  $c$  and  $r$ .

`RMSE` computes the root mean squared error of the predictions. `PlotPredictions` and `PlotResiduals` plot the predictions or their residuals; `PlotStdResiduals` and `PlotQQ` plot the standardized residuals.

**Examples**

```
borehole_pred <- Predict(
  GaSP_model = borehole_fit,
  x_pred = borehole$x_pred,
  generate_coefficients = TRUE
)
```

---

 RMSE

---

*Calculate the root mean squared error (RMSE) of prediction*


---

**Description**

Calculate the root mean squared error (RMSE) of prediction

**Usage**

```
RMSE(y_pred, y_true, normalized = FALSE)
```

**Arguments**

<code>y_pred</code>	A vector of predicted output values.
<code>y_true</code>	A vector of true output values.
<code>normalized</code>	An optional boolean: if TRUE, the RMSE is normalized by dividing it by the standard deviation of <code>y_true</code> .

**Value**

The RMSE or normalized RMSE.

**Examples**

```
RMSE(borehole_pred$y_pred$Pred, borehole$y_true)
```

```
RMSE(borehole_cv$Pred, y)
```

---

 Visualize

*Visualize a GaSPModel object.*


---

### Description

Carry out a functional analysis of variance (ANOVA) of a `GaSPModel` object and generate plotting coordinates for its estimated main and 2-input joint effects.

### Usage

```
Visualize(GaSP_model, x_description, main_percent = 0, interaction_percent = 0)
```

### Arguments

<code>GaSP_model</code>	Object of class <a href="#">GaSPModel</a> .
<code>x_description</code>	A data frame describing the input variables. See <a href="#">DescribeX</a> .
<code>main_percent</code>	An optional minimum percentage of variation explained by an input's main effect to return the effect's plotting coordinates; the default of zero gives plotting coordinates for all inputs.
<code>interaction_percent</code>	An optional minimum percentage of variation explained by the interaction effect of a pair of inputs to return the plotting coordinates for their joint effect (main effects plus interaction effect); the default of zero gives plotting coordinates for all pairs of inputs.

### Details

If there are many inputs, to avoid excessive plotting of many trivial joint effects set `interaction_percent = 1` say.

### Value

A list with the following elements:

<code>anova_percent</code>	A data frame containing the ANOVA percentages for all main effects and 2-input interaction effects.
<code>main_effect</code>	A data frame with plotting coordinates for the estimated main effects.
<code>joint_effect</code>	A data frame with plotting coordinates for the estimated 2-input joint effects.
<code>total_percent</code>	Total percentage of the prediction variation accounted for by all main effects and 2-input interaction effects.
<code>average</code>	Overall average of the prediction function, averaged with respect to all inputs.
<code>SE_average</code>	Standard error of the overall average.

**References**

Schonlau, M. and Welch, W.J. (2006), "Screening the Input Variables to a Computer Model Via Analysis of Variance and Visualization", in *Screening: Methods for Experimentation in Industry, Drug Discovery, and Genetics*, Dean. A. and Lewis, S., eds., pp. 308-327, Springer, New York, doi:10.1007/0-387-28014-6\_14.

**Examples**

```
borehole_vis <- Visualize(borehole_fit, borehole_x_desc)
```

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